

Part 1

# Polygons

(The new notes)

What is a figure?

→ A geometric form consisting of point, lines, curved lines & planes

↓                      ↓                      ↓                      ↓

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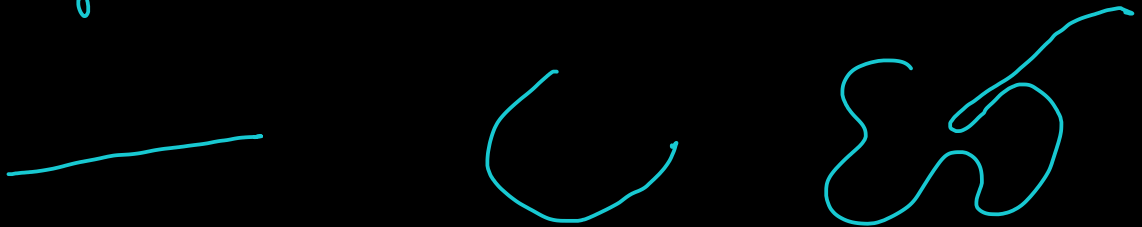
ignore pls. ↑

Types of figure :

• CLOSED :- They are closed



• OPEN :- They are open

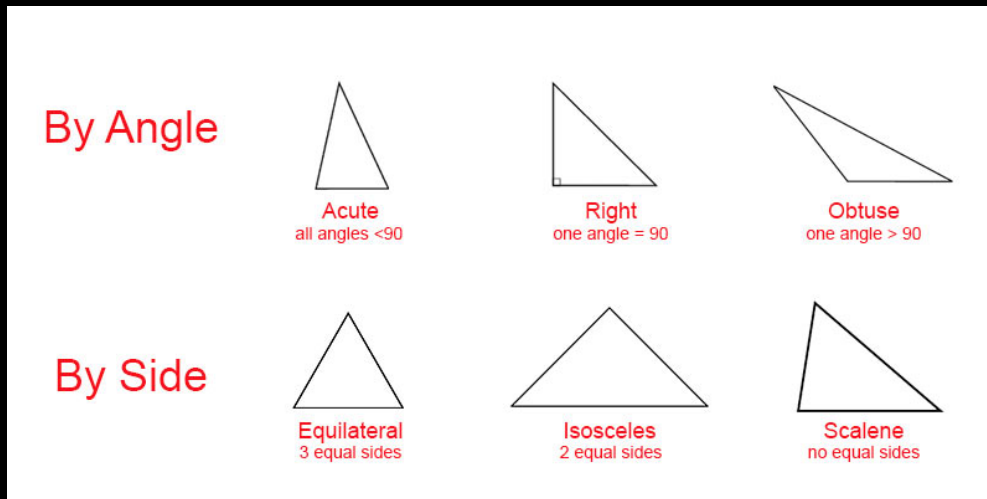


POLYGONS :-

- Closed figure with straight edges  
(circle is not a polygon)

# Types of Polygons :-

- Triangle



- Quadrilateral

## Types of Quadrilaterals



parallel lines

lines which never intersect

opposite sides equal and parallel

Quadrilateral	Shape
Square	
Rectangle	
Parallelogram	
Trapezium	
Rhombus	
Kite	

→ All sides equal and all angles =  $90^\circ$

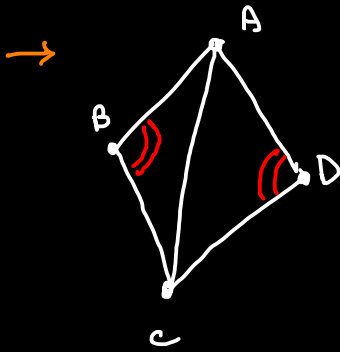
→ Opposite sides equal and parallel and all angles =  $90^\circ$

→ One pair of sides parallel

→ all sides equal, diagonals are perpendicular to each other

→  $AB = AD, BC = DC$

Q. In a rhombus, opposite angles are equal  
(same way for parallelogram)



In  $\triangle ABC$ ,  $\triangle ADC$

$$AB = AD$$

$$BC = DC$$

$$AC = AC$$

[rhombus has all 4 sides equal]

Hence by SSS congruency,

$$\triangle ABC \cong \triangle ADC$$

$$\Rightarrow \angle ABC = \angle ADC$$

$$\text{Similarly } \angle BAD = \angle BCD$$

Adjacent sides

Any two sides with a common end point are called the adjacent sides of the polygon.

Adjacent vertices

The end points of the same side of a polygon are called the adjacent vertices.

Diagonals

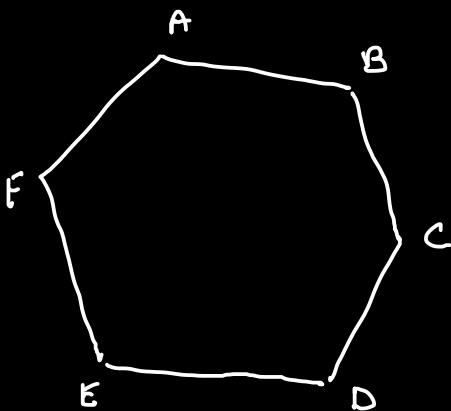
The line segments obtained by joining vertices which are not adjacent are called the diagonals of a polygon.

Concave polygon:

If a diagonal lies outside a polygon, then the polygon is called a concave polygon.

Convex polygon:

If all the diagonals lie inside the polygon, then the polygon is said to be a convex polygon.

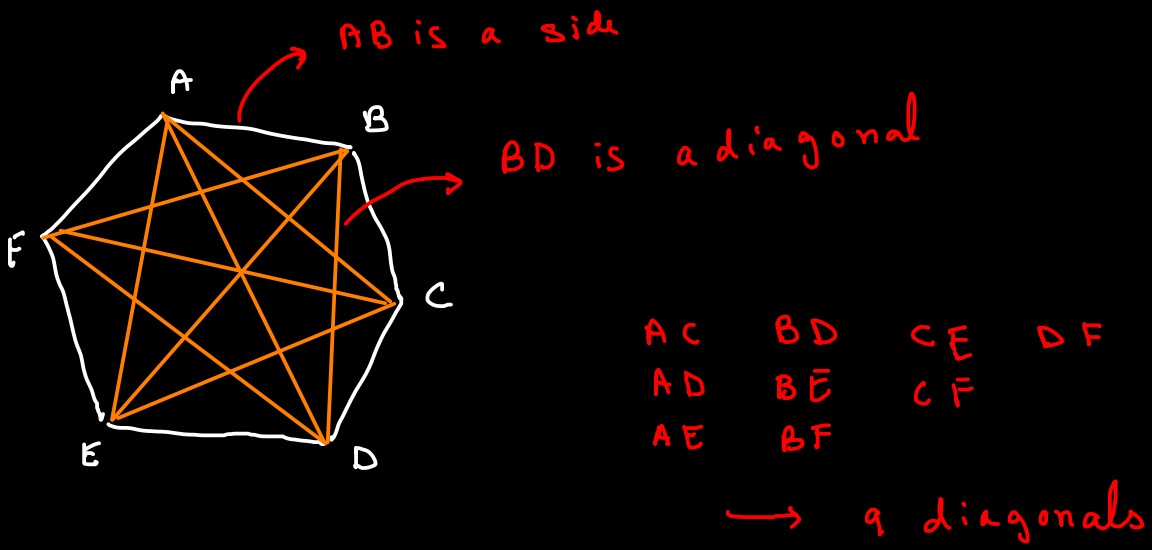


• A, B are adjacent vertices (side AB)

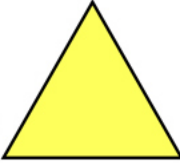

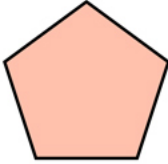

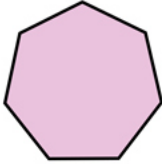


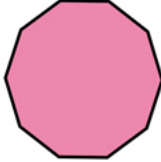
• A, D are not adjacent

↪ AB, BC are adjacent

↘ ED, BC are not adjacent



## Types of Polygons

<p><b>Triangle</b></p> <ul style="list-style-type: none"> <li>• Has 3 sides and 3 vertices</li> <li>• Has no diagonals</li> <li>• Sum of the interior angles is <math>180^\circ</math></li> </ul> 	<p><b>Quadrilateral</b></p> <ul style="list-style-type: none"> <li>• Has 4 sides and 4 vertices</li> <li>• Has two diagonals</li> <li>• Sum of the interior angles is <math>360^\circ</math></li> </ul> 
<p><b>Pentagon</b></p> <ul style="list-style-type: none"> <li>• Has 5 sides and 5 vertices</li> <li>• Has 5 diagonals</li> <li>• Sum of the interior angles is <math>540^\circ</math></li> </ul> 	<p><b>Hexagon</b></p> <ul style="list-style-type: none"> <li>• Has 6 sides and 6 vertices</li> <li>• Has 9 diagonals</li> <li>• Sum of the interior angles is <math>720^\circ</math></li> </ul> 
<p><b>Heptagon</b></p> <ul style="list-style-type: none"> <li>• Has 7 sides and 7 vertices</li> <li>• Has 14 diagonals</li> <li>• Sum of the interior angles is <math>900^\circ</math></li> </ul> 	<p><b>Octagon</b></p> <ul style="list-style-type: none"> <li>• Has 8 sides and 8 vertices</li> <li>• Has 20 diagonals</li> <li>• Sum of the interior angles is <math>1080^\circ</math></li> </ul> 
<p><b>Nonagon</b></p> <ul style="list-style-type: none"> <li>• Has 9 sides and 9 vertices</li> <li>• Has 27 diagonals</li> <li>• Sum of the interior angles is <math>1260^\circ</math></li> </ul> 	<p><b>Decagon</b></p> <ul style="list-style-type: none"> <li>• Has 10 sides and 10 vertices</li> <li>• Has 35 diagonals</li> <li>• Sum of the interior angles is <math>1440^\circ</math></li> </ul> 

$n$ -gon for  $n \geq 12$ .

No of diagonals in  $n$ -gon:


$$\text{No of diagonals in } n\text{-gon} = \frac{n(n-3)}{2}$$

Proof: -

- Now we can choose a vertex in  $n$  different ways ( $n$  vertices)
- each vertex is endpoint of  $n-3$  diagonals (why? try a few examples)
- So the number of diagonals =  $n(n-3)$
- However every diagonal is counted 2 times

So we must divide by 2. (why?)

• Hence  $\frac{n(n-3)}{2}$

↪ because  any diagonal has 2 endpoints

P.S. Try verifying for a few values

(we verified in the class)